

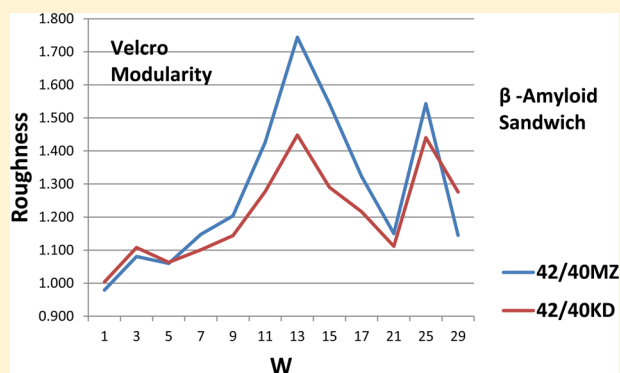
## Thermodynamic Description of Beta Amyloid Formation Using Physicochemical Scales and Fractal Bioinformatic Scales

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**ABSTRACT:** Protein function depends on both protein structure and amino acid (aa) sequence. Here we show that modular features of both structure and function can be quantified economically from the aa sequences alone for the small (40,42 aa) plaque-forming (aggregative) amyloid beta fragments. Some edge and center features of the fragments are predicted. Bioinformatic scales based on  $\beta$  strand formation propensities and the thermodynamically second order fractal hydrophobicity scale based on evolutionary optimization (self-organized criticality) are contrasted with the standard first order physicochemical scale based on complete protein (water–air) unfolding. The results are consistent with previous studies of these physicochemical factors that show that aggregative properties, even of beta fragments, are driven primarily by near-equilibrium hydrophobic forces.

**KEYWORDS:** Protein, function, amino acid, sequence, evolutionary, criticality, self-organized



The amyloid precursor protein APP of Alzheimer's disease (AD) (details available on Uniprot as P05067) has 770 amino acids (aa) and resembles a cell surface receptor. Two small amyloid fragments of A4 ( $A\beta$  40, 672–711 and  $A\beta$  42, 672–713) form plaques. Monomer fragments aggregate to form successive oligomeric globules, proto-fibers, or fibers, with the latter being most toxic. An NMR structural model<sup>1</sup> shows that the cores of these fragments are dominated by a  $\beta$  sandwich structure with halves,  $\beta_1 = 18$ –26 and  $\beta_2 = 31$ –40 or 31–42, connected by a  $\beta$  turn stabilized by an (E22,D23)-K28 double salt bridge. A hydrophilic loop 1–17 connects successive monomers (Figure 1, from ref 1).

Presently evidence suggests that oligomer intermediates, which lead to fibril formation, may be the primary culprits leading to neuronal dysfunction and cell death.<sup>2</sup> Numerous studies have suggested<sup>3–10</sup> that  $A\beta$  42 is more toxic than  $A\beta$  40. The molecular origin of the biological differences between  $A\beta$  40 and 42 is still under study.<sup>2,11</sup>

Here we examine nonlocal hydrophobic  $A\beta$  40 and 42 interactions within a modular framework in which ability to identify both the length scale of the  $\beta$  sandwich structure (Figure 1) and describe the biological differences between  $A\beta$  40 and 42 is used to evaluate the relative importance of different physicochemical factors in describing protein aggregation. Before the bioinformatic scales used here were available, the aggregative properties of lysozyme *c* and acylphosphatase had been previously studied using single amino acid mutagenesis. Distinct chemical factors influence protein properties, and one of the easier general properties to study is aggregation. Reference 12 showed for these two proteins, which are nearly centrosymmetric with respect to their  $\alpha/\beta$  structures, that mutated aggregation rates depend on

two leading properties: hydrophobicity, and the difference between  $\alpha$  helicity and  $\beta$  strand propensities. The first two factors were estimated from empirical aa enthalpy-transfer tables, and it was concluded that globular hydrophobic compaction dominates secondary  $\alpha/\beta$  propensities. Is this conclusion still true for the strikingly pure  $\beta$  sandwich structure (Figure 1)?

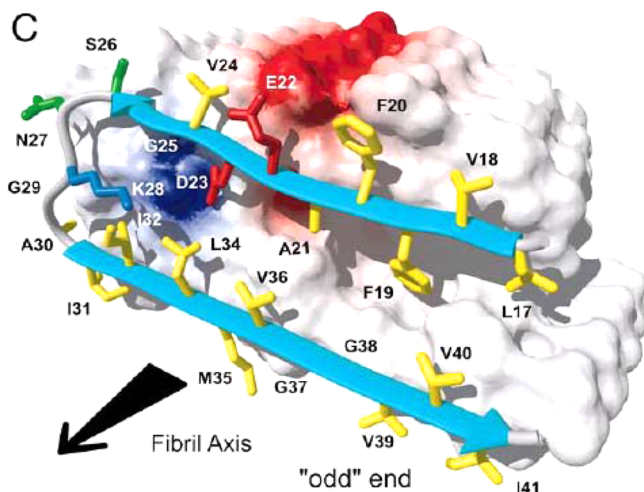
In earlier papers,<sup>13–17</sup> we discussed the thermodynamic significance of the standard (15 000+ citations) water–air, first-order, enthalpy-based KD hydrophobicity scale.<sup>18</sup> The new MZ hydrophobicity scale, based on self-organized criticality (SOC), was derived bioinformatically from the differential solvent-exposed geometry of >5000 protein segments.<sup>19</sup> Its derivation strongly suggests second-order character, suitable for describing modular conformational activity, which should dominate most protein functionality. Earlier results from correlations between evolutionary trends in functionalities and aa sequences generally showed better agreement using the MZ scale compared to the KD scale. The evolution of lysozyme *c*, from zebrafish through chickens and mammals to humans, is especially instructive, for its centrosymmetric separation of modular structures into  $\alpha$  helix and  $\beta$  strand domains.<sup>14</sup> Mutations in lysozyme *c* are associated with amyloidosis.<sup>14</sup>

Recently bioinformatic scales of  $\alpha$  helicity and  $\beta$  strand propensities, separated into different values for exposed and buried residues, have appeared, based again on surveys of

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**Figure 1.** van der Waals contact surface polarity and ribbon diagram of the 17–42 residues of  $A\beta$  (Reproduced from Figure 4 of ref 1. Volumes 90–105 (1993–2008) copyright © by the National Academy of Sciences). The 13-mer modular sandwiched  $\beta$ -sheets are indicated by cyan arrows, and the hydrophobic amino acid side chains are shown in yellow. Positively and negatively charged surface patches are shown in blue and red, respectively, with the D23-K28 (E22) salt bridge. The N-terminal hydrophilic loop 1–16 (672–687), which connects successive fibrillar molecules, is disordered and is not resolved by NMR solution data.

thousands of PDB structures.<sup>20</sup> Can these propensity scales recognize the 13-mer sandwich structure (Figure 1)?

Earlier work comparing the two  $\psi(aa,1)$  hydrophobicity scales often examined the variance (or roughness)  $\mathcal{R}$  of modular sequences  $\psi(aa,W)$ , where  $\psi(aa,W)$  is  $\psi(aa,1)$  averaged over a sliding window of width  $W = 2N + 1$ :

$$\psi(n, W) = \text{average}[\psi(n - N), \psi(n + N)]$$

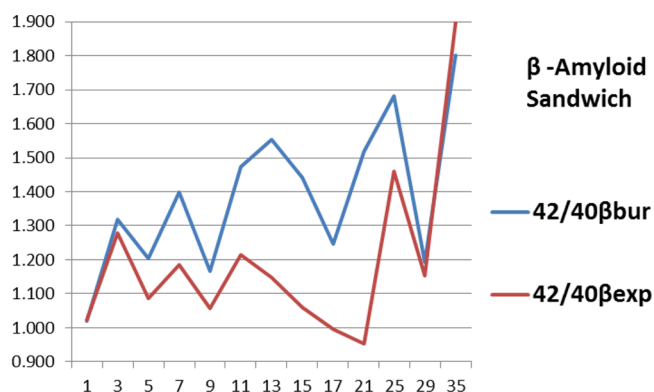
$$\mathcal{R}(W) = \text{average}[\psi(n, W) - \text{average}[\psi(n, W)]]^2$$

The intuitive interpretation of  $W$  is that it represents the length of a modular element that dominates the protein functionality. The nature of this modular element is especially clear for the amyloid precursor protein A4, whose critical step is fragmentation into  $A\beta$  40 or  $A\beta$  42, here often renumbered as 1–40 or 1–42, respectively. We were able to identify a thermodynamic spinodal, analogous to (P,V) spinodals of elementary van der Waals (vdW) gas–liquid phase diagrams, by identifying two closely spaced weak breaks in slope of the KD  $\mathcal{R}(\psi(aa,W))$ , and two widely spaced larger breaks in slope of the MZ  $\mathcal{R}(\psi(aa,W))$ . This shows that the MZ scale corresponds to a lower effective temperature than the KD scale. It explains why the MZ scale gave better correlations between evolutionary trends in functionalities and aa sequences than the KD scale for many other proteins.<sup>21</sup>

Given the A4 spinodal, we also saw that the modular width  $W$  is analogous to the molar volume  $V_m$ , and  $\mathcal{R}$  is analogous to the pressure  $p$  in gas–liquid equations of state, such as the vdW equation. Modularity emerges spontaneously in aa distributions of primitive proteins.<sup>22</sup> One can recognize multiple pairwise hydrophobicity correlations statistically.<sup>23</sup> Here we have shown that very detailed properties for a given protein can be identified using thermodynamic variables  $W$  and  $\mathcal{R}$  derived from aa using hydrophobicity scales.

## RESULTS AND DISCUSSION

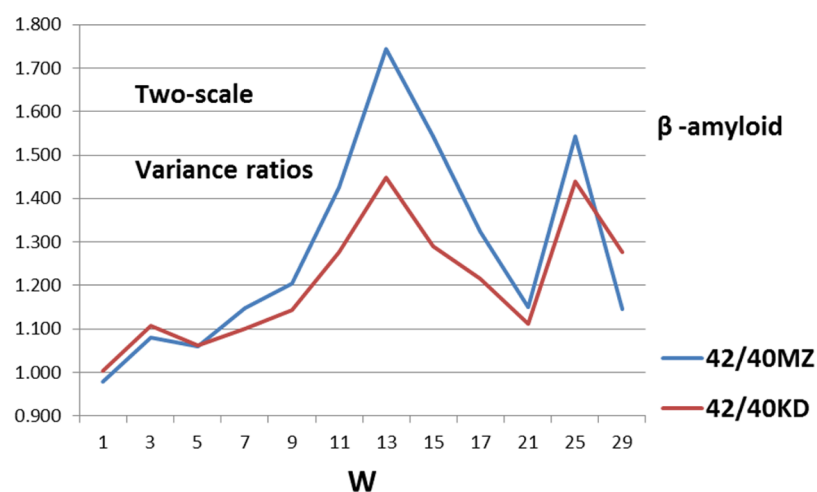
The amyloid fragments  $A\beta$  occur in the 40 aa left half of the compound C-terminal hydrophobic peak.<sup>21</sup> This 80 aa peak is strongly hydrophobic, and rises well above the profile of the rest of A4. It is also about four times as long as a typical 20 aa transmembrane segment of a GPCR protein.<sup>15</sup> It splits in half to form the 40aa  $A\beta$  including  $\beta_1 = 18$ –26 and  $\beta_2 = 31$ –40 or 31–42 fragments, which then self-organize into plaque. One can also connect the 40 aa C-terminal half peak width to the 42aa width of the spinodal tie line between  $W = 19$  and  $W = 61$  in the log–log plot of  $\mathcal{R}(W)$  for A4, Figure 2.<sup>21</sup>



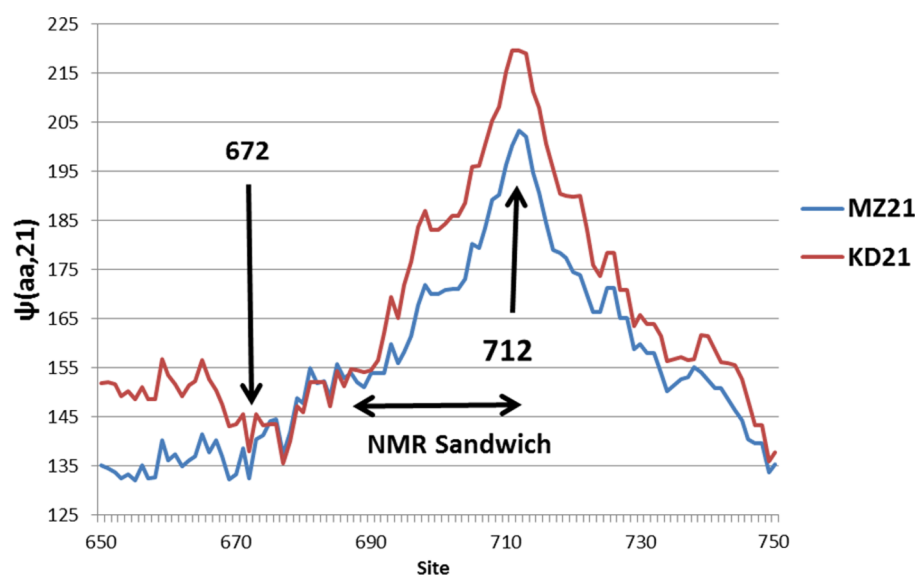
**Figure 2.** Roughness or variance  $\mathcal{R}(W) = \langle \langle \psi(aa,W) \rangle \rangle^2 - \langle \langle \psi(aa,W) \rangle \rangle^2$  of amyloid  $\beta$  fragments as a function of the sliding window length  $W$ . Because  $A\beta$  40 is much less toxic (aggregative) than  $A\beta$  42,  $\mathcal{R}(W)$  of the latter is normalized by  $\mathcal{R}(W)$  of the former. There is complex structure in the buried residue  $\beta$  strand plot that can be interpreted as primarily 13- and 26-mers, but the overall  $\beta$  strand profile is noisy.

In Figure 2, we show the roughness ratios  $\mathcal{R}_{42}(W)/\mathcal{R}_{40}(W)$  for two kinds of  $\beta$  strand propensities, exposed and buried. The buried profile shows complex structure, which is suggestive of the sandwich structure of Figure 1, but is not so easily interpreted. By contrast, Figure 3 shows the same ratios using the traditional enthalpy transfer scale KD<sup>18</sup> and the modern differential surface area scale MZ.<sup>19</sup> The improvement between Figures 2 and 3 is dramatic, and it scarcely can be explained as either accidental or artificial, as  $\mathcal{R}(W)$  has been used often by us for other proteins.<sup>13–15,17</sup>

It is indeed remarkable that such a strikingly simple scaling pattern, resembling diffraction, can result from hydrophobicity scales alone. As shown in Figure 2, hydrophobic modularity is unambiguous, with peaks at  $W = W_{\max} = 13$ , and harmonics at  $W = 27$ , with both MZ and KD scales. It is striking that the differential MZ scale based on SOC (second-order phase transition) is twice as effective as the complete unfolding (first-order) KD scale in identifying  $W_{\max}$ . This confirms previous results for the MZ superiority found in other larger proteins.<sup>13–15,17</sup> It is easy to see that  $W_{\max}$  should be 13, as this divides  $A\beta$  into three nearly equal parts, the hydrophilic loop, and the two hydrophobic  $\beta_1$ – $\beta_2$  strands. While there may be hundreds of hydrophobic scales, this test can be applied to any hydrophobic scale, however defined. The superiority of the MZ scale is expected to persist, because it is based on a bioinformatic survey of >5000 protein segments,<sup>19</sup> but the present results can be easily falsified by improving them with some other scale, a task which lies outside the scope of this discussion.



**Figure 3.** Roughness or variance  $\mathcal{R}(W) = \langle \langle \psi(aa,W)^2 \rangle \rangle - \langle \langle \psi(aa,W) \rangle \rangle^2$  of amyloid  $\beta$  fragments as a function of the sliding window length  $W$ . Because  $A\beta$  40 is much less toxic (aggregative) than  $A\beta$  42,  $\mathcal{R}(W)$  of the latter is normalized by  $\mathcal{R}(W)$  of the former. Note that simply comparing the values of  $\mathcal{R}(1)$  fails, and that the strongest  $W = 13$  modularity peak of the sandwiched  $\beta$ -sheets is resolved well even with the KD scale. The MZ scale resolves the modular structure much better than the  $\beta$  strand propensity scale in Figure 1. It also produces a strongest peak that is almost twice as large when  $W$  is tuned to 13.



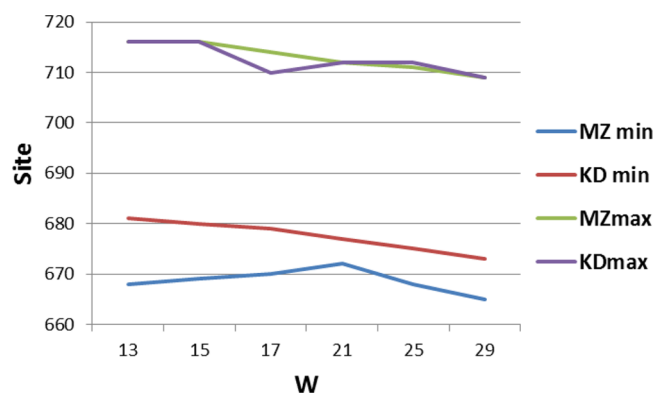
**Figure 4.** Detail of the wide A4 hydrophobic peak of  $\psi(aa,21)$ . The beginnings of the amyloid fragments occur just at the hydrophilic cleavage dip at Asp672, and end at the hydrophobic peak  $712 \pm 1$ . The flat top of KD21 spans 711–713. It may therefore be said that the KD scale correctly identifies the first-order separation of  $A\beta$ 40 from  $A\beta$ 42 (the splitting of  $712 \pm 1$ ). It is possible that the 3 aa width of this KD flat peak is accurate because fragmentation occurs at a high effective temperature.<sup>17</sup> The range covered by the NMR sandwich model of Figure 1 matches the abrupt increases of the MZ and KD  $\psi(aa,21)$  profiles near site 688.

The detailed KD and MZ  $W = 21$  profiles show how this connection occurs at the 672 beginning of the hydrophilic loop (Figure 4). As noted in ref 21,  $W = W_c = 21$  is a natural choice for the modular  $W$  in the vdW equation of state, but it is especially suited to describing A4 fragmentation between 671 and 672 by the membrane-bound enzyme secretase family.<sup>24</sup> Both scales show that the  $A\beta$  fragments are strongly amphiphilic,<sup>25</sup> with the left end located at a hydrophilic minimum for  $W = 21$ , and the right end at a hydrophobic maximum.

The MZ success achieved with  $W = 21$  in predicting the 672 and  $712 \pm 1$  cleavage sites is unique. Figure 5 shows the results with other choices of modular length  $W$ . These yield extrema near, but not at, the experimental cleavage sites. Profile extrema drift due to numerical noise is natural in such complex proteins,

which suggests that the successes achieved with  $W = 21$ , and particularly the MZ scale, is thermodynamic in nature and derives from the lower effective temperature associated with the MZ scale.

The variance or roughness  $\mathcal{R}(W) = \langle [\psi(aa,W)]^2 \rangle - [\langle \psi(aa,W) \rangle]^2$  measures the effective pressure  $p$  exerted by the “ball bearing” roughness of the protein’s water package as it slides and/or tumbles into successive conformations. A simple macroscopic model for the hydrophobic  $\beta$  sandwich shown in Figure 1 supposes that the  $\beta$ 1 and  $\beta$ 2 strands are stabilized both by the  $\beta$  turn and by mechanical velcro-like roughness of intra- and intersandwich packing under the influence of water pressure. In other words, the larger the roughness, the greater the sandwich, oligomer, and fibril thermal stabilization. This



**Figure 5.** Amphiphilic extrema of  $\psi(\text{aa},W)$  profiles in the  $A\beta$  range. Figure 2 showed the  $\psi(\text{aa},21)$  profiles. This figure shows that the 672 “disordered” cleavage site is predicted correctly by hydrophilic maxima only with the MZ scale and  $W = 21$ . The  $712 \pm 1$  cleavage site is predicted correctly by hydrophobic maxima with the KD scale for  $W = 21$  and 25, and with the MZ scale for  $W = 21$ .

also explains the remarkable success of the MZ scale in Figure 3.

The differences between the KD complete unfolding scale, and the MZ differential or conformational scale, are neither accidental nor incidental. The associated profiles of  $\psi(\text{aa},13)$  are shown in Figure 6. The MZ scale reflects the differences between the hydrophilic loop (1–17) and the hydrophobic sandwich strands 18–42 more accurately, which in turn more accurately resolves the modular structure functionality, including even softer hydrophilicity for the hairpin turn, with the MZ scale. Similar plots for  $W = 9$  and  $W = 17$  (not shown) are less informative, as expected from Figure 3.

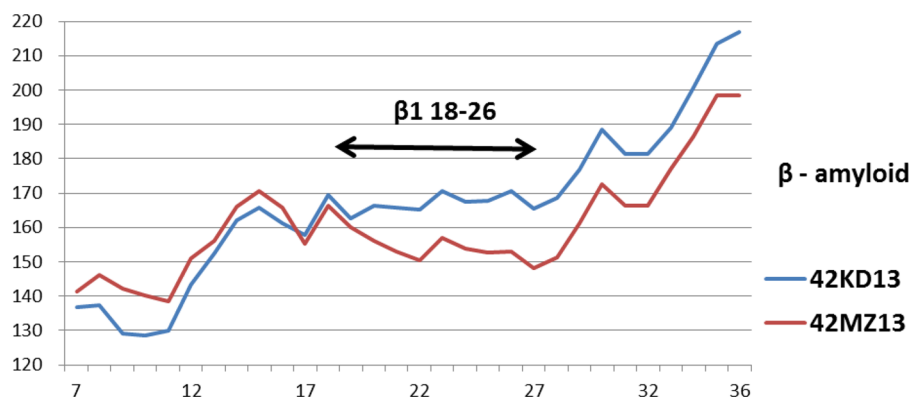
In discussing A4 (770 aa), we used spinodal breaks to argue<sup>21</sup> that the MZ scale measures fragmentation at a lower effective temperature. One can still define effective temperatures for the  $A\beta$  40/42 fragments from the values of  $\mathcal{R}(W)$  for the two scales. This gives effective temperature or  $\mathcal{R}(W)$  ratios of KD/MZ ranging from 1.67 ( $W = 13$ ) to 1.93 ( $W = 21$ ). These  $\mathcal{R}(W)$  ratios are sensible for two reasons: (1) the effective temperatures of the KD scale are higher than those for the MZ scale, and (2) fragmentation is best described by  $W = 21$ , where the  $\mathcal{R}(W)$  ratio is larger and the effective temperatures are higher, and sandwich reconstruction and aggregation is best

described by  $W = 13$  (Figure 3), where the  $\mathcal{R}(W)$  ratio is smaller and the effective temperatures are lower.

There are many  $A\beta$  familial mutations, and even in vitro these exhibit a wide range of oligomer and fibrous morphologies.<sup>1</sup> Some of these can be explained by roughness changes, with success similar to that achieved by other means, including atomic force microscopy and molecular dynamics. The A673T mutation that reduces  $\beta$  cleavage<sup>26</sup> broadens the hydrophilic minimum centered on Asp 672 (Figure 4), which could explain reduced effectiveness of secretase cleavage.

Our analysis of the  $\beta$  fragments, which are only  $\sim 40$  aa long, has confirmed the central conclusion of our earlier thermodynamic analysis<sup>21</sup> of A4 (770 aa). Simple algebraic analysis, using only amino acid sequences, has revealed thermodynamically significant aspects of plaque formation, and distinguished essential features of small (40,42 aa) plaque-forming amyloid  $\beta$  fragments. In the present case, an amphiphilic velcro model has emerged for the  $\beta$  amyloid fragments that may encompass some other  $\beta$  strand structures as well. The amphiphilic features<sup>27</sup> that distinguish the weak  $\beta_1 = 18$ –26 and strong  $\beta_2 = 31$ –40 or 31–42 hydrophobic  $\beta$ -sheet surfaces on the thermodynamics and kinetics of the polymerization process<sup>28</sup> are quantified. We have also found consistent values of effective temperatures, which are frequently used to describe the thermodynamic properties of glasses and deeply supercooled liquids.<sup>28,29</sup> We have also utilized the full power of bioinformatic methods to test independently the central conclusion of many earlier papers (such as ref 12), that aggregative properties are driven mainly by hydrophobic forces, and not secondary structures, here even for pure  $\beta$  sandwiches.

More generally, large-scale structure is recognizable as modules in the community structures of both biological and nonbiological networks that are self-organized.<sup>30</sup> The present thermodynamic method utilizes protein sequence evolution and recognizes modular structures without detailed knowledge of protein folding,<sup>31</sup> and thus provides a remarkably effective and economical tool for connecting sequences to function. The example of amyloid sandwich fragments is a successful functional illustration of protein fractal symmetry.<sup>32</sup> It also shows that the fractal scale is most suitable for irreversible large-scale protein aggregation as well as equilibrium properties, such as describing cytoskeletal actin networks in motile cells as critically self-organized systems.<sup>33</sup>



**Figure 6.** Profiles of  $\psi(\text{aa},13)$  for  $A\beta_{42}$  for the MZ SOC differential scale and the first-order KD scale, renumbered with 672 = 1. Note the hydrophilic softening of  $\beta_1$  at the hairpin turn (26–30, see Figure 1) with the SOC MZ scale. This  $\beta_1$  softening facilitates formation of the modular sandwich structure, by making its central region more flexible. At the hairpin turn, the  $W = 13$  profile with the KD scale is nearly flat, but there is a local soft hydrophilic minimum promoting a mechanical hinge in the MZ profile at 27.

Proteolytic cleavage of APP is driven mainly by more than 150 presenilin mutations. Some time ago, researchers were puzzled by the fact that experimentally reduction of the cleavage rate with fewer mutations increases the concentration ratio of A $\beta$ 42/A $\beta$ 40; conventionally, this is described as “loss of function”.<sup>34</sup> This mystery is resolved by Figure 3. Fewer mutations slow the cleavage rate and bring one closer to equilibrium, and in equilibrium the natural fragment is A $\beta$  42. Various solutions to this mystery were proposed, including elaborate multichannel, multistage cleavages. The present model (Figure 3) shows (without elaborate mechanisms) that this mysterious effect is merely the result of kinetics near thermodynamic equilibrium.

## METHODS

The MZ and KD scaling parameters are tabulated in ref 13. The calculations were made using an EXCEL macro written by Niels Voohoeve and refined by Douglass C. Allan.

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### Notes

The authors declare no competing financial interest.

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